

```

[ y:=sin(3);
[ sin(3)
[ ex:=2*a*sin(x/y);
  prog::exptree(ex)

2 a sin( $\frac{x}{\sin(3)}$ )
  _mult
  |
  +-- a
  |
  +-- sin
  |
  |   \-- _mult
  |       |
  |       +-- x
  |       |
  |       \-- _power
  |           |
  |           +-- sin
  |               |
  |               \-- 3
  |               |
  |               \-- -1
  |
  \-- 2
Tree1
[ nops(ex);
[ 3
[ op(ex,1);
[ a
[ op(ex,2);
[ sin( $\frac{x}{\sin(3)}$ )
[ op(ex,3);
[ 2
[ op(ex,[2,1]);
[  $\frac{x}{\sin(3)}$ 
[ domtype(2);
[ DOM_INT

```

```
domtype(2/3);
DOM_RAT
domtype(0.5);
DOM_FLOAT
domtype(FALSE);
DOM_BOOL
domtype(ex)
DOM_EXPR
domtype(x);
DOM_IDENT
x:=1+i;
1+i
domtype(x);
DOM_COMPLEX
s:="this is a string";
"this is a string"
domtype(s);
DOM_STRING
s2:="also this";
"also this"
s.s2;
"this is a stringalso this"
s[3..6]
"is i"
reset();
k:=4;
4
y.k:=99;
99
y4;
```

```

[ 99
[   f:=-x^2;
[   -x^2
[ domtype(f)
[   DOM_EXPR
[ g:=x->-x^2;
[   x → -x^2
[ domtype(g);
[   DOM_PROC
[ f(2);
[   -x(2)^2
[ g(2) ;
[   -4
[ h:=(x,y)->x^2+y^2;
[   (x, y) → x^2 + y^2
[ h(1,2);
[   5
[   myabs:=x->if x>=0 then x else -x end_if;
[   x → (if 0 <= x then x el...
[   myabs(3);
[   3
[   myabs(-3);
[   3
[   g2:=x->x+2;
[   x → x+2
[   w:=g2@g;
[   (x → x+2) ◦ (x → -x^2)
[   w(2);
[   -2
[   u:=x-->f;
[   x → -x^2
[   u(2);

```

```

-4
TRUE or UNKNOWN;
TRUE
TRUE and UNKNOWN;
UNKNOWN
not bool(1=2);
TRUE
not bool(1<>2) ;
FALSE
set:={a,1,3,x->4};
{1, 3, a, x → 4}
nops(set);
4
set2:={a,3};
{3, a}
set union set2;
{1, 3, a, x → 4}
set intersect set2;
{3, a}
set minus set2;
{1, x → 4}
contains(set,1);
TRUE
g:=x->-x^2;
x → -x2
map(set2,g);
{-9, -a2}
g2:=x->bool(x>0);
x → bool(0 < x)

```

```

[ a:=-4;
[ -4
[ select(set2,g2);
[ {3}
[ seq:=1,a,TRUE;
[ 1, -4, TRUE
[ domtype(seq);
[ DOM_EXPR
[ nops(seq);
[ 3
[ op(seq,3);
[ TRUE
[ seq[3];
[ TRUE
[ seq2:=i^2 $ i=1..6;
[ 1, 4, 9, 16, 25, 36
[ 2 $ 10;
[ 2, 2, 2, 2, 2, 2, 2, 2, 2, 2
[ sin(x) $ x in [0,PI,2];
[ 0, 0, sin(2)
[ seq3:=seq,seq2;
[ 1, -4, TRUE, 1, 4, 9, 16, 25, 36
[ domtype(null());
[ DOM_NULL
[ seq[2]:=2,3;
[ 2, 3
[ seq;
[ 1, 2, 3, TRUE
[ delete seq[2];
[ seq;
[ 1, 3, TRUE
[

```

```
[ max(seq2);
[ 36
[ min(seq2) ;
[ 1
[ lst:=[1,a,TRUE];
[ [1, -4, TRUE]
[ domtype(lst);
[ DOM_LIST
[ nops(lst);
[ 3
[ op(lst,3);
[ TRUE
[ lst[3];
[ TRUE
[ lst2:=[];
[ []
[ lst3:=lst.[r,y];
[ [1, -4, TRUE, r, y]
[ [a,b,c]:=[1,2,3];
[ [1, 2, 3]
[ a:=1;
[ 1
[ b:=2;
[ 2
[ [a,b]:=[b,a];
[ [2, 1]
[ a;
[ 2
[ b;
[ 1
[ contains(lst,1);
[ 1
[ map([x,1,0],sin);
[ [sin(x), sin(1), 0]
```

```
sort([4,7,-2]);
```

```
[-2, 4, 7]
```

```
select([4,7,-2],g2);
```

```
[4, 7]
```

```
x:=1;
```

```
1
```

```
for i from 1 to 5 do
```

```
x:=x+i;
```

```
end_for;
```

```
16
```

```
y:=1;
```

```
1
```

```
for i from 1 to 5 step 2 do
```

```
y:=y+i;
```

```
end_for
```

```
10
```

```
reset();
```

```
myFact:= proc(n)
```

```
begin ;
```

```
f:=1;
```

```
for i from 2 to n do
```

```
f:=f*i;
```

```
end_for;
```

```
return(f);
```

```
end_proc;
```

```
myFact(3)
```

```
proc myFact(n) ... end
```

```
6
```

```
reset();
```

```
test1:=proc(n)
```

```
begin
```

```
primes:=select([$2..floor(n/2)],isprime);
```

```
lst:=[n $ nops(primes)] - primes;
```

```
good:=select(lst,isprime);
```

```
return (bool(nops(good)>0));
```

```
end_proc;
```

```
proc test1(n) ... end
```

```
n:=500;
```

```
500
```

```
l:=[2*i $ i=2..floor(n/2)];
```

```
[4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28, 30, 32, 34, 36, 38, 40, 42, 44, 46, 48, 50, 52, 54, 56,
58, 60, 62, 64, 66, 68, 70, 72, 74, 76, 78, 80, 82, 84, 86, 88, 90, 92, 94, 96, 98, 100, 102, 104, 106,
108, 110, 112, 114, 116, 118, 120, 122, 124, 126, 128, 130, 132, 134, 136, 138, 140, 142, 144, 146,
148, 150, 152, 154, 156, 158, 160, 162, 164, 166, 168, 170, 172, 174, 176, 178, 180, 182, 184, 186,
188, 190, 192, 194, 196, 198, 200, 202, 204, 206, 208, 210, 212, 214, 216, 218, 220, 222, 224, 226,
228, 230, 232, 234, 236, 238, 240, 242, 244, 246, 248, 250, 252, 254, 256, 258, 260, 262, 264, 266,
268, 270, 272, 274, 276, 278, 280, 282, 284, 286, 288, 290, 292, 294, 296, 298, 300, 302, 304, 306,
308, 310, 312, 314, 316, 318, 320, 322, 324, 326, 328, 330, 332, 334, 336, 338, 340, 342, 344, 346,
348, 350, 352, 354, 356, 358, 360, 362, 364, 366, 368, 370, 372, 374, 376, 378, 380, 382, 384, 386,
388, 390, 392, 394, 396, 398, 400, 402, 404, 406, 408, 410, 412, 414, 416, 418, 420, 422, 424, 426,
428, 430, 432, 434, 436, 438, 440, 442, 444, 446, 448, 450, 452, 454, 456, 458, 460, 462, 464, 466,
468, 470, 472, 474, 476, 478, 480, 482, 484, 486, 488, 490, 492, 494, 496, 498, 500]
```

```
select(1,not test1);
```

```
[]
```

```
constructor:=Dom::IntegerMod(7);
```

```
Dom::IntegerMod(7)
```

```
x:=constructor(3);
```

```
3 mod 7
```

```
y:=constructor(5);
```

```
5 mod 7
```

```
domtype(x);
```

```
Dom::IntegerMod(7)
```

```
x+y;
```

```
1 mod 7
```

```
x*y;
```

```
1 mod 7
```

```
x^123;
```

```
6 mod 7
```

```
reset();
```

```
p:=poly(1+a*x+3*x^2,[x]);
```

```
poly(3 x2 + a x + 1, [x])
```

```
domtype(p);
```

```
DOM_POLY
```

```
p|x=2;
```

```
2 a + 13
```

```
degree(p,x);
```

```
2
```



```

[ coeff(p, 2);
  3
[ list:=[[1, 0], [a, 3], [b, 5]];
  [[1, 0], [a, 3], [b, 5]]
[ p2:=poly(list, [x]);
  poly(b x^5 + a x^3 + 1, [x])
[ poly2list(p);
  [[3, 2], [a, 1], [1, 0]]
[ p3:=poly(x+1, [x]);
  poly(x + 1, [x])
[ p+p3;
  poly(3 x^2 + (a + 1) x + 2, [x])
[ p*p3;
  poly(3 x^3 + (a + 3) x^2 + (a + 1) x + 1, [x])
[ divide(p, p3);
  poly(3 x + a - 3, [x]), poly(-a + 4, [x])
[ factor(p*p3);
  poly(x + 1, [x]) poly(3 x^2 + a x + 1, [x])
[ gcd(p, p3);
  poly(1, [x])
[ D(p);
  poly(6 x + a, [x])
[ int(p);
  poly(x^3 + a/2 x^2 + x, [x])
[ p4:=poly(4*x+11, [x], Dom::IntegerMod(3));
  poly(x + 2, [x], Dom::IntegerMod(3))
[ domtype(p4);
  DOM_POLY
[ p4|x=2;
  1 mod 3
[ reset();
  A:=matrix([[1, 2, 3, 4],
  [a, b, c, d],
  [sin(x), cos(x), exp(x), ln(x)]]);
  (
    ( 1    2    3    4
      a    b    c    d
    sin(x) cos(x) e^x ln(x) )

```

```

Dom::Matrix();
Dom::Matrix()

v:=matrix([[x1],[x2],[x3],[x4]]);

$$\begin{pmatrix} x1 \\ x2 \\ x3 \\ x4 \end{pmatrix}$$


A*v;

$$\begin{pmatrix} x1 + 2 x2 + 3 x3 + 4 x4 \\ a x1 + b x2 + c x3 + d x4 \\ x2 \cos(x) + x3 e^x + x4 \ln(x) + x1 \sin(x) \end{pmatrix}$$


A[2,3];
c

A[2,3]:=4;
4

A[1..2,2..3];

$$\begin{pmatrix} 2 & 3 \\ b & 4 \end{pmatrix}$$


transpose(A);

$$\begin{pmatrix} 1 & a & \sin(x) \\ 2 & b & \cos(x) \\ 3 & 4 & e^x \\ 4 & d & \ln(x) \end{pmatrix}$$


diff(A,x);

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ \cos(x) & -\sin(x) & e^x & \frac{1}{x} \end{pmatrix}$$


int(A,x);

$$\begin{pmatrix} x & 2x & 3x & 4x \\ ax & bx & 4x & dx \\ -\cos(x) & \sin(x) & e^x & x(\ln(x) - 1) \end{pmatrix}$$


map(A,x->x^2);

$$\begin{pmatrix} 1 & 4 & 9 & 16 \\ a^2 & b^2 & 16 & d^2 \\ \sin(x)^2 & \cos(x)^2 & e^{2x} & \ln(x)^2 \end{pmatrix}$$


constructor:=Dom::Matrix(Dom::Rational);
Dom::Matrix(Dom::Rational)

A:=constructor(2,3);

$$\begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$


```

```
B:=constructor([[1,2,3],[1,2,3]]);
```

$$\begin{pmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \end{pmatrix}$$

```
C:=constructor(2,3,(i,j)->i*j);
```

$$\begin{pmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \end{pmatrix}$$

```
constructor(2,2,[11,12],Diagonal);
```

$$\begin{pmatrix} 11 & 0 \\ 0 & 12 \end{pmatrix}$$

```
constructor::identity(2);
```

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

```
constructor2:=Dom::SquareMatrix(2);
```

$$\text{Dom::SquareMatrix}(2)$$

```
A:=constructor2([[0,y],[x^2,1]]);
```

$$\begin{pmatrix} 0 & y \\ x^2 & 1 \end{pmatrix}$$

```
domtype(A);
```

$$\text{Dom::SquareMatrix}(2)$$

```
A^(-1);
```

$$\begin{pmatrix} -\frac{1}{x^2 y} & \frac{1}{x^2} \\ \frac{1}{y} & 0 \end{pmatrix}$$

```
exp(A);
```

$$\begin{pmatrix} \frac{\sigma_1 - \sigma_2 + \sigma_1 \sigma_3 + \sigma_2 \sigma_3}{\sigma_3^2} & \frac{\sigma_1 - \sigma_2 - \sigma_1(4yx^2 + 1) + \sigma_2(4yx^2 + 1)}{x^2 \sigma_3^4} \\ -\frac{x^2 \sigma_1 - x^2 \sigma_2}{\sigma_3} & \frac{-\sigma_1 + \sigma_2 + \sigma_1 \sigma_3 + \sigma_2 \sigma_3}{\sigma_3^2} \end{pmatrix}$$

where

$$\sigma_1 = e^{-\frac{\sigma_3}{2} + \frac{1}{2}}$$

$$\sigma_2 = e^{\frac{\sigma_3}{2} + \frac{1}{2}}$$

$$\sigma_3 = \sqrt{4yx^2 + 1}$$

```
con:=Dom::Matrix(Dom::Rational);
```

```
Dom::Matrix(Dom::Rational)
```

```
H:=con(15,15,(i,j)->1/(i+j+1));
```


$$\begin{pmatrix} 2040 \\ -171360 \\ 5290740 \\ -84651840 \\ 814773960 \\ -5121436320 \\ 22086194130 \\ -67310305920 \\ 147241294200 \\ -232016584800 \\ 261018657900 \\ -204434193600 \\ 105867707400 \\ -32574679200 \\ 4508102925 \end{pmatrix}$$

```
DIGITS:=100;
```

```
100
```

```
con:=Dom::Matrix(Dom::Rational);
```

```
Dom::Matrix(Dom::Rational)
```

```
M:=Dom::Matrix(Dom::Rational);
```

```
Dom::Matrix(Dom::Rational)
```

```
H:=con(3,3,(i,j)->1/(i+j+1));
```

$$\begin{pmatrix} \frac{1}{3} & \frac{1}{4} & \frac{1}{5} \\ \frac{1}{4} & \frac{1}{5} & \frac{1}{6} \\ \frac{1}{5} & \frac{1}{6} & \frac{1}{7} \end{pmatrix}$$

```
M:=col(H,2);
```

$$\begin{pmatrix} \frac{1}{4} \\ \frac{1}{5} \\ \frac{1}{6} \end{pmatrix}$$

```
M:=row(H,2);
```

$$\left(\frac{1}{4} \frac{1}{5} \frac{1}{6} \right)$$

```
M:=delCol(H,2);
```

$$\begin{pmatrix} \frac{1}{3} & \frac{1}{5} \\ \frac{1}{4} & \frac{1}{6} \\ \frac{1}{5} & \frac{1}{7} \end{pmatrix}$$

```
M:=delRow(H,2);
```

$$\begin{pmatrix} \frac{1}{3} & \frac{1}{4} & \frac{1}{5} \\ \frac{1}{5} & \frac{1}{6} & \frac{1}{7} \end{pmatrix}$$

```
M:=matdim(H);
```

```
[3, 3]
```

```

M::tr(H);

$$\frac{71}{105}$$

M::transpose(H);

$$\begin{pmatrix} \frac{1}{3} & \frac{1}{4} & \frac{1}{5} \\ \frac{1}{4} & \frac{1}{5} & \frac{1}{6} \\ \frac{1}{5} & \frac{1}{6} & \frac{1}{7} \end{pmatrix}$$

M::identity(6);

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

A:=M(2,2,[[1,2],[3,1]]);

$$\begin{pmatrix} 1 & 2 \\ 3 & 1 \end{pmatrix}$$

linalg::det(A);
-5
linalg::charpoly(A,y);
 $y^2 - 2y - 5$ 
linalg::eigenvalues(A);
 $\emptyset$ 
M:=Dom::Matrix(Dom::Float);
Dom::Matrix(Dom::Float)
A:=M(2,2,[[1,2],[3,1]]);

$$\begin{pmatrix} 1.0 & 2.0 \\ 3.0 & 1.0 \end{pmatrix}$$

linalg::eigenvalues(A);
{-1.449489742783178098197284074705891391965947480656670128432692567250960377457315026\
539859433104640235, 3.449489742783178098197284074705891391965947480656670128432692567\
250960377457315026539859433104640235}
linalg::eigenvectors(A);
[[[3.4494897427831780981972840747058913919659474806566701284326925672509603774573150265\
39859433104640235, 1, [[0.63245553203367586639977870888654370674391102786504336537150\
0970558518887727847644268849621675860059],
[0.774596669241483377035853079956479922166584341058318165317514753222696618387395806\
7038574753717347036]]], [-1.44948974278317809819728407470589139196594748065667012843\
2692567250960377457315026539859433104640235, 1, [[-0.6324555320336758663997787088865\
43706743911027865043365371500970558518887727847644268849621675860059],
[0.774596669241483377035853079956479922166584341058318165317514753222696618387395806\
7038574753717347036]]]]]
linalg::nullspace(A);
[]
a:=matrix([[1,2],[3,5]]);

```

```

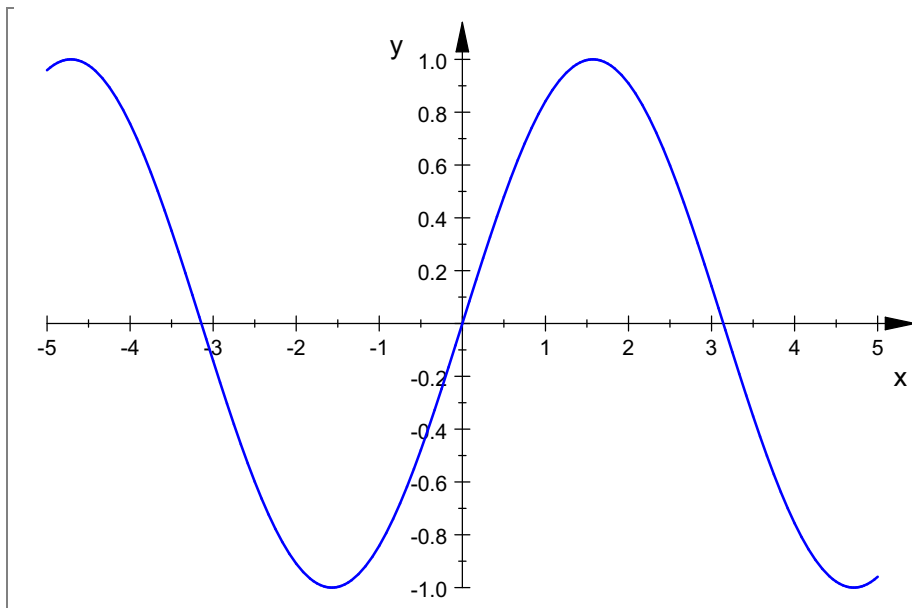
[ (1 2)
  (3 5)
det(a);
-1
numeric::det(a);
-1.0
linalg::eigenvalues(a);
{3 - sqrt(10), sqrt(10) + 3}
numeric::eigenvalues(a);
[6.16227766016837933199889354443271853371955513932521682685750485279259443863923822134\
4248108379300295, -0.162277660168379331998893544432718533719555139325216826857504852\
792594438639238221344248108379300295]
reset();
f:=1/(exp(x^2)+1);
1
e^{x^2} + 1
g:=diff(f,x);
- 2 x e^{x^2}
(e^{x^2} + 1)^2
int(g,x);
1
e^{x^2} + 1
int(g,x=0..PI);
1
e^{\pi^2} + 1} - 1/2
p:=exp(-x^2);
e^{-x^2}
int(p,x=-0..5);
sqrt(pi) erf(5)
2
simplify( (exp(x)-1)/(exp(x/2)+1) );
e^{x/2} - 1
simplify((cos(x))^2+(sin(x))^2);
1
limit(sin(x)/x,x=0);
1
limit((1+1/n)^n,n=infinity);
e
sum(i,i=1..n);

```

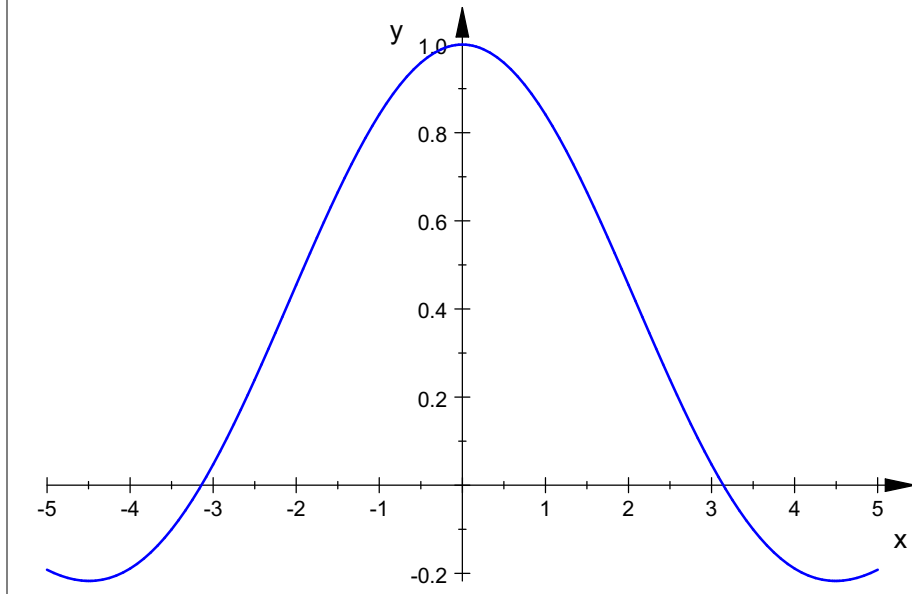
```

[  $\frac{n(n+1)}{2}$ 
[ sum(1/i^2,i=1..infinity);
[  $\frac{\pi^2}{6}$ 
[ product(i^3,i=1..n);
[  $n!^3$ 
[ eqn:={x+y=a,x-a*y=b};
[ {x+y=a,x-a*y=b}
[ solve(eqn,{x,y});
[  $\left\{ \begin{array}{l} \left\{ \left[ x = \frac{a^2+b}{a+1}, y = \frac{a-b}{a+1} \right] \right\} \text{ if } a \neq -1 \\ \{[x = -z - 1, y = z]\} \text{ if } a = -1 \wedge b = -1 \\ \emptyset \text{ if } a = -1 \wedge b \neq -1 \end{array} \right.$ 
[ solve(x*exp(x)=x,{x});
[ (x) ∈ {(2 π k i) | k ∈ ℤ}
[ solve(x*exp(x)=x,{x},Real);
[ {[x=0]}
[ die := random(1..6);
[ proc random() ... end
[ die() $ i = 1..20 ;
[ 4, 3, 4, 6, 5, 3, 6, 3, 2, 2, 2, 4, 4, 3, 3, 2, 1, 4, 4, 6
[ n := stats::normalRandom(1,3);
[ proc n() ... end
[ n() $ i = 1..20;
[ 0.08246332598, 0.01372971472, 0.1060112816, -0.889346086, 4.087416217, 2.103373604,
[ 2.195520634, 1.588855508, 3.039834827, -0.03415436006, -1.401051242, -0.694503791,
[ -0.36683284, 1.362125436, 1.378762055, -0.2803558955, 2.125162477, 2.084038475,
[ 7.247328352, 0.4250666925
[ u := stats::uniformRandom(1,3);
[ proc u() ... end
[ u() $ i = 1..20 ;
[ 2.835443688, 2.705667995, 1.040935403, 1.364254937, 2.76328391, 2.516756717, 2.075771544,
[ 2.341294666, 2.536763713, 2.814471874, 1.893579666, 2.702989494, 1.788103892, 1.771497027,
[ 1.548483545, 1.414521647, 2.19508155, 2.455392566, 1.819040605, 2.673157143
[ plot(sin(x));

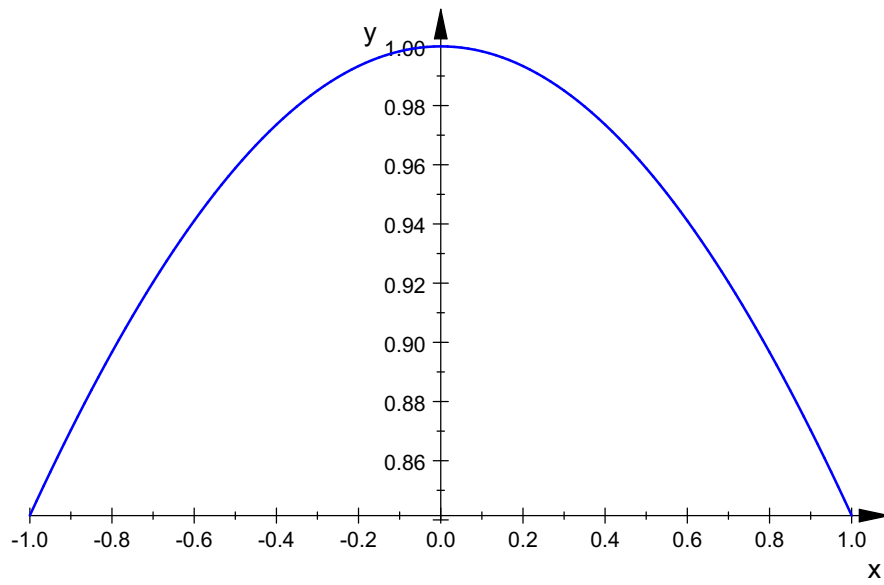
```

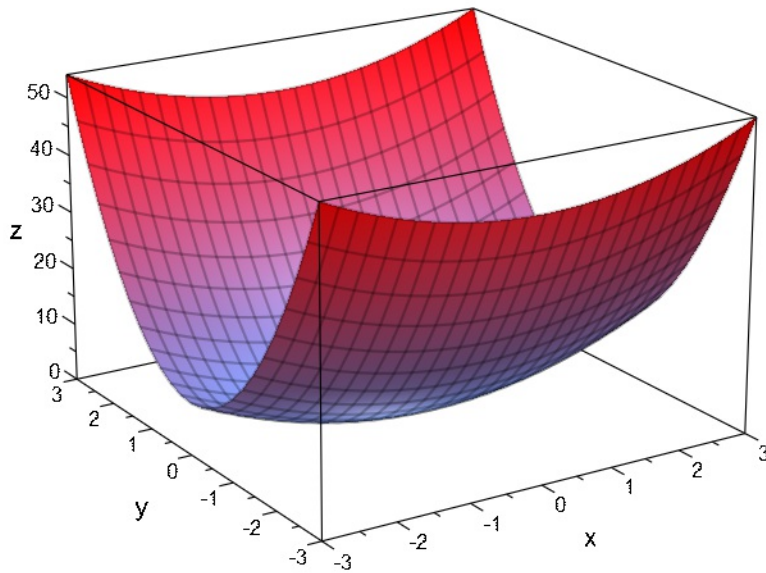
```
plot(sin(x)/x);
```



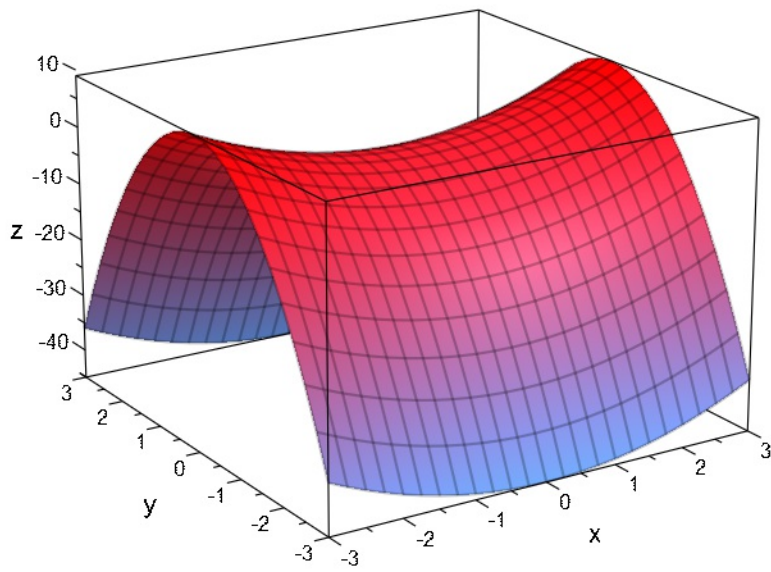
```
plot(sin(x)/x,x=-1..1);
```



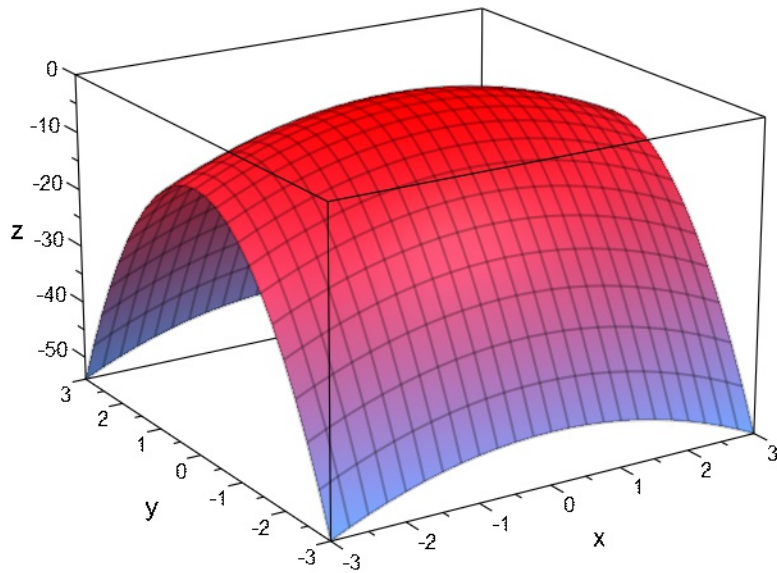
```
plot(x^2+5*y^2,x=-3..3,y=-3..3,#3D);
```



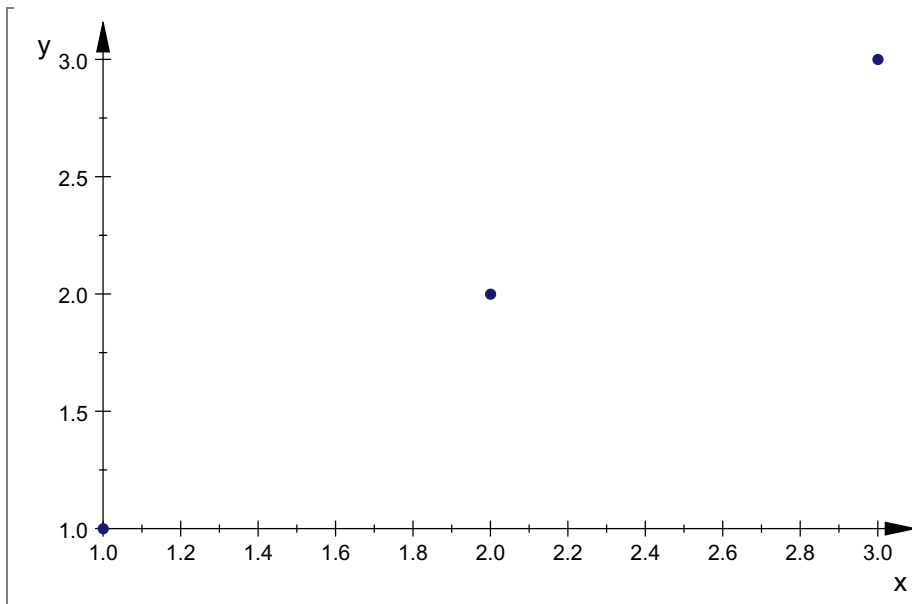
```
plot(x^2-5*y^2,x=-3..3,y=-3..3,#3D);
```



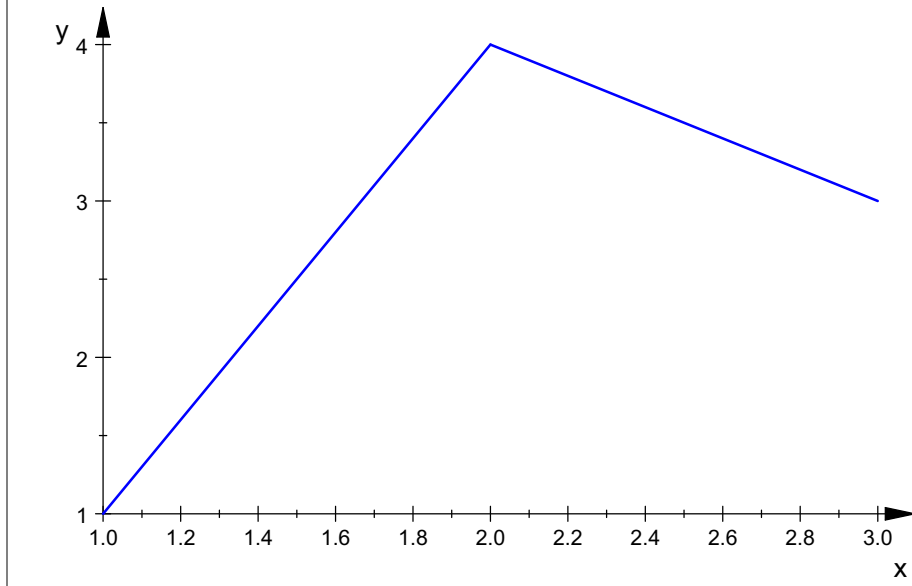
```
plot(-x^2-5*y^2,x=-3..3,y=-3..3,#3D);
```



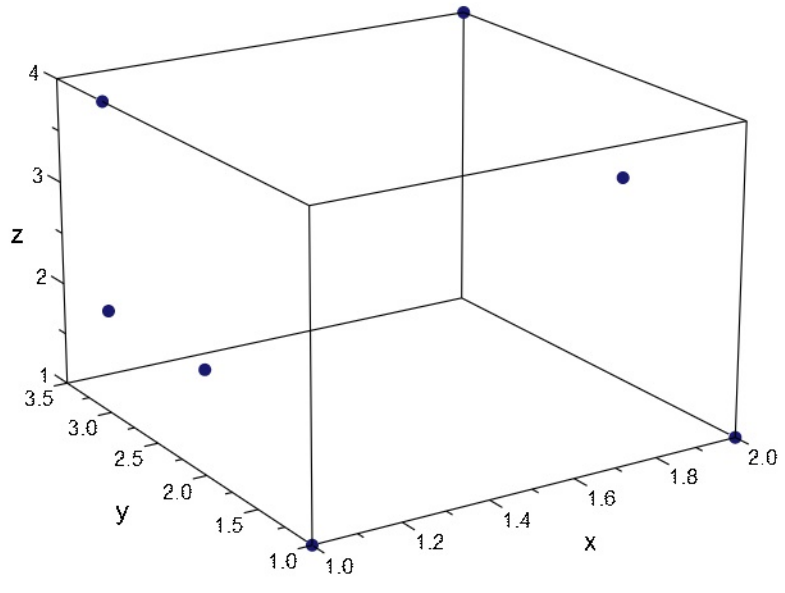
```
plot(plot::PointList2d([[1,1],[2,2],[3,3]]));
```



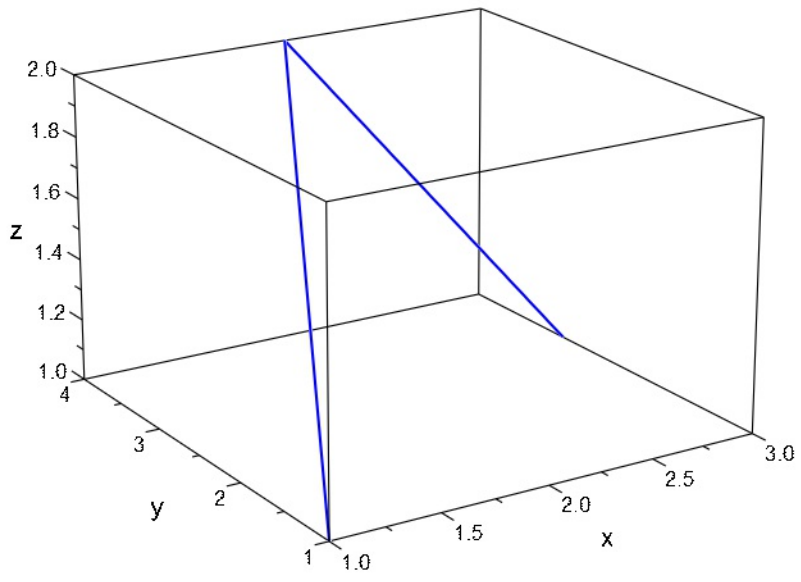
```
plot(plot::Polygon2d([[1,1],[2,4],[3,3]]));
```



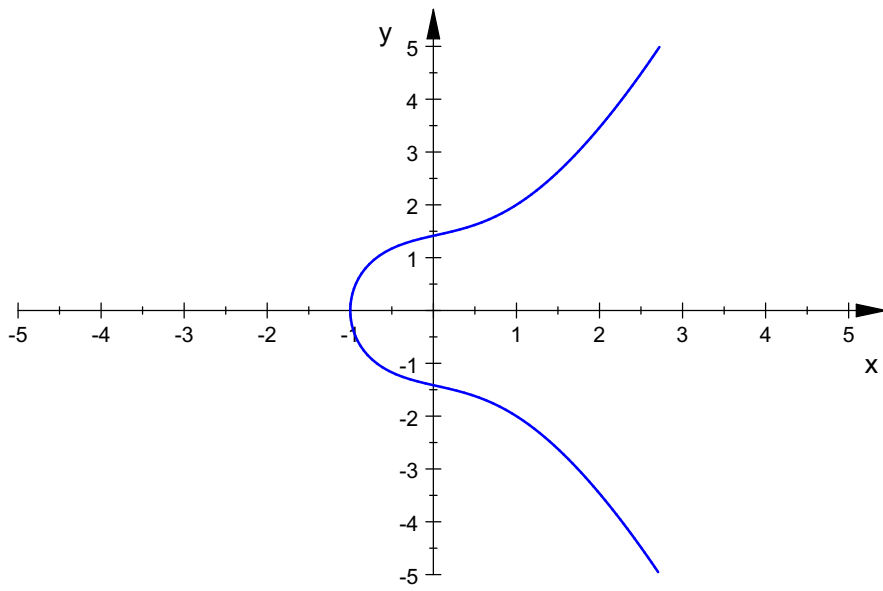
```
plot(plot::PointList3d([[1,1,1], [1,2,2], [1,3,2], [1,3,4],  
[2,1,1], [2,2,3], [2,3.5, 4]],PointSize=5));
```



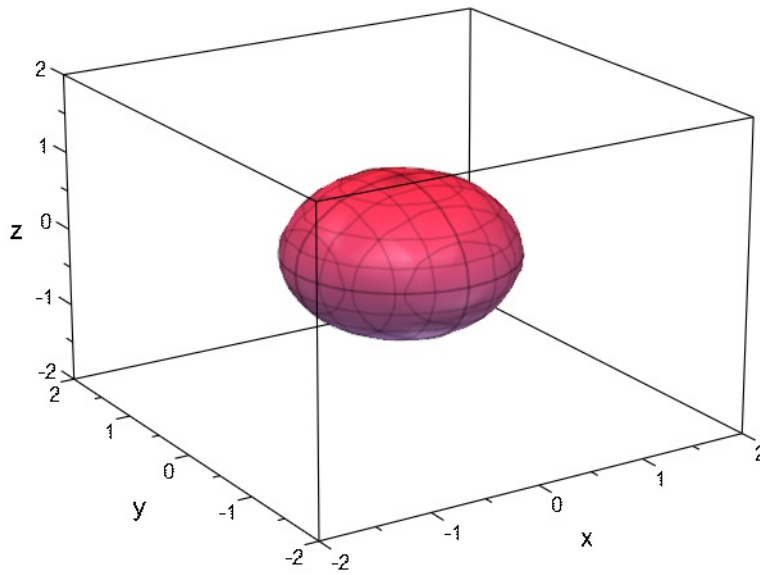
```
plot(plot::Polygon3d([[1,1,1],[2,4,2],[3,3,1]]));
```



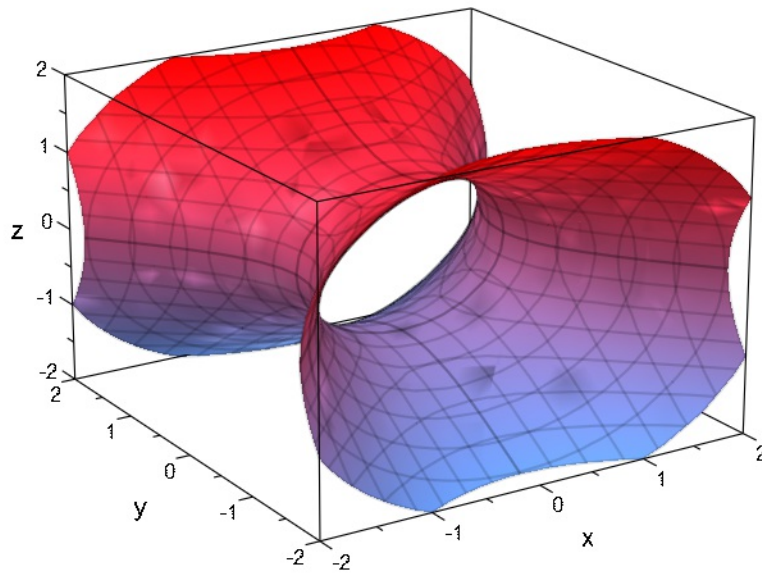
```
plot(plot::Implicit2d(x^3 + x + 2 = y^2,x = -5..5, y = -5..5));
```



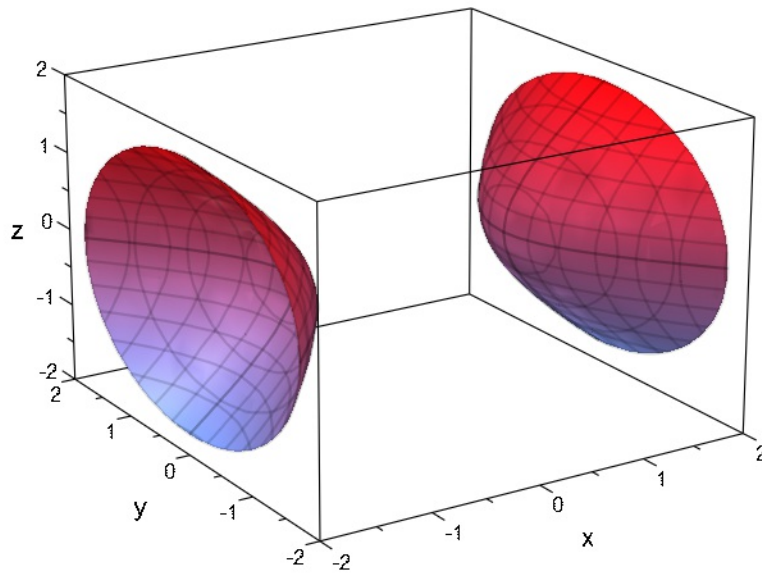
```
plot(plot::Implicit3d(x^2+y^2+z^2=1,x=-2..2,y=-2..2,z=-2..2));
```



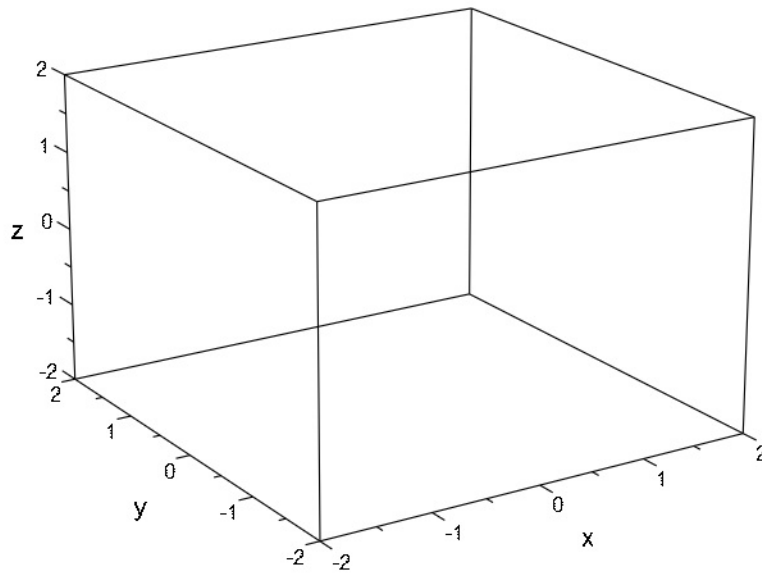
```
plot(plot::Implicit3d(x^2-y^2+z^2=1,x=-2..2,y=-2..2,z=-2..2));
```



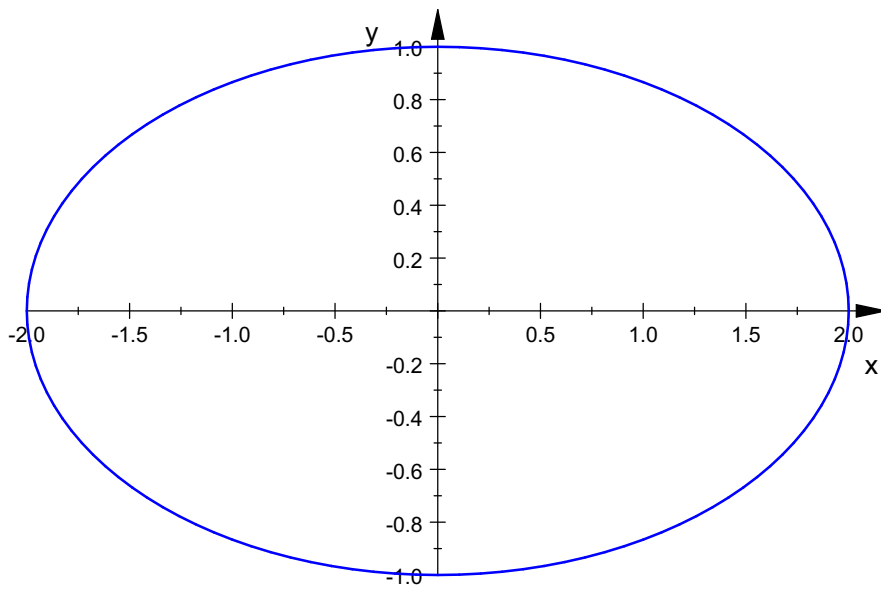
```
plot(plot::Implicit3d(x^2-y^2-z^2=1,x=-2..2,y=-2..2,z=-2..2));
```



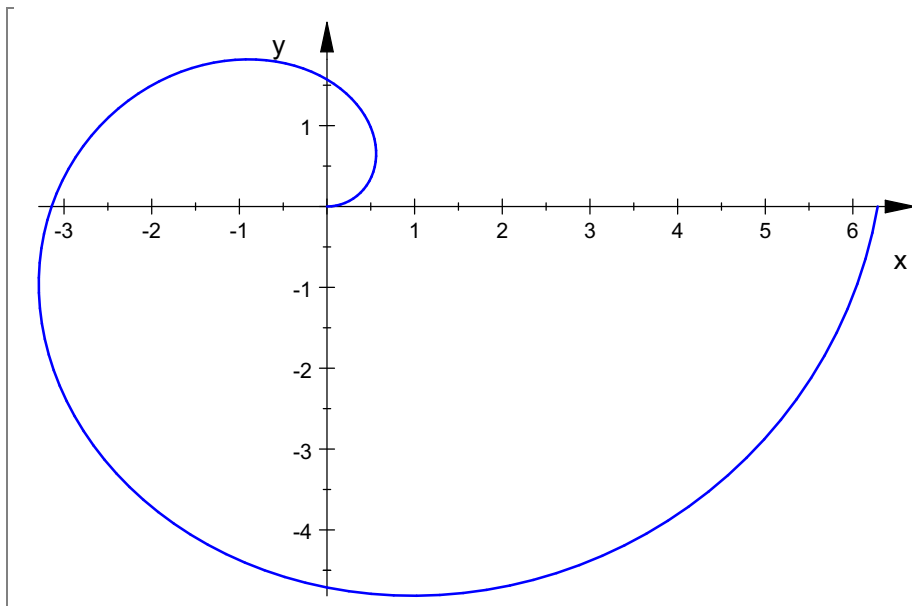
```
plot(plot::Implicit3d(-x^2-y^2-z^2=1,x=-2..2,y=-2..2,z=-2..2));
```



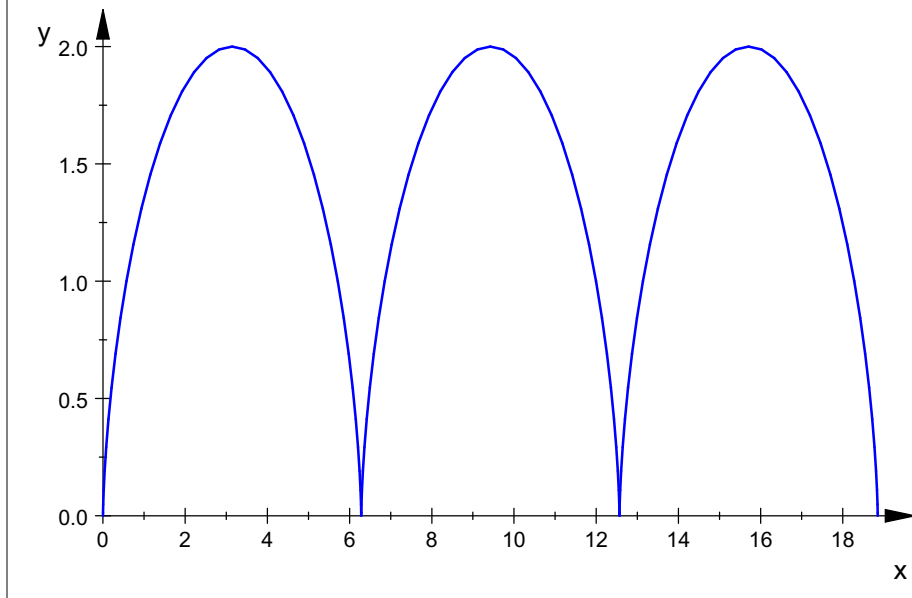
```
plot([2*cos(t), sin(t)], t=0..2*PI);
```



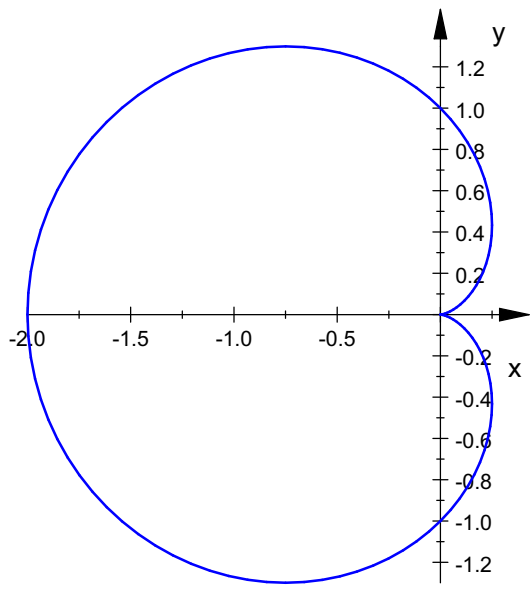
```
plot([t*cos(t), t*sin(t)], t=0..2*PI);
```

```
plot([t-sin(t),1-cos(t)],t=0..6*PI) ;
```



```
plot(plot::Polar([1-cos(t),t],t=0..2*PI));
```



[
[